

# Quantifying Surface and Internal Charging Parameters Through Flying Virtual Satellites in the RAM-SCB Inner Magnetosphere Model

**Sorin Zaharia, D. T. Welling, V. K. Jordanova and R. H. W. Friedel**

**Los Alamos National Laboratory  
Los Alamos, NM 87545**

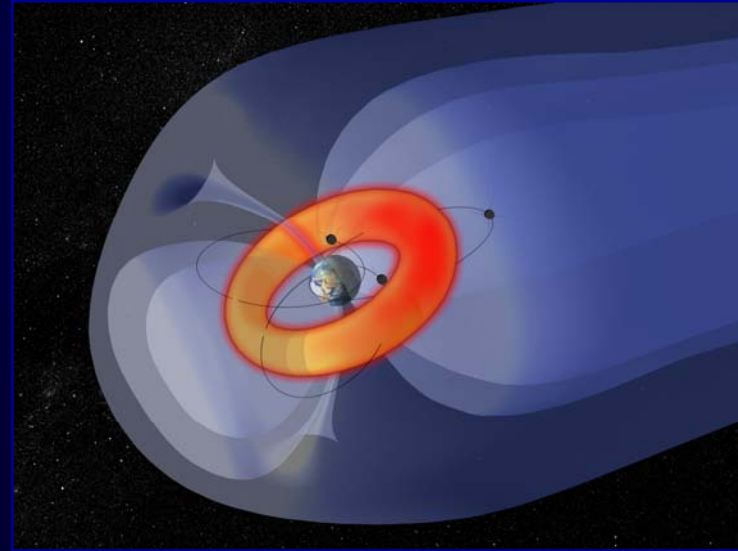
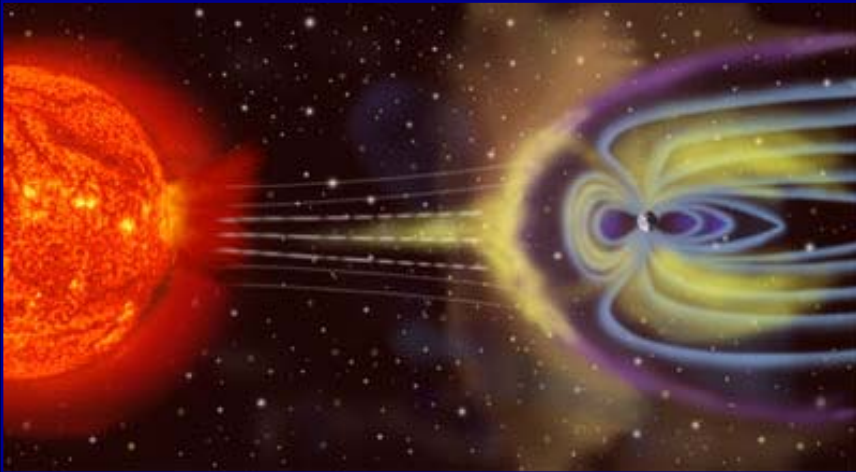
*11<sup>th</sup> Spacecraft Charging Technology Conference (SCTC)*

*Albuquerque, NM, September 24, 2010*

# Outline

- Goal: quantifying the ambient environment along satellite orbit, relevant to spacecraft charging, by “flying” virtual satellites in model domain
- Physics-based model: Ring Current Atmosphere Interactions Model with Self-Consistent Magnetic (B) field (RAM-SCB)
  - Importance of interaction between particles and fields
  - Can be driven by global model (e.g. SWMF) or data-driven (e.g. LANL)
  - Full 3-D and pitch angle anisotropy
  - Particles include contributors to both surface and internal charging
- Results: RAM-SCB geomagnetic storm simulation
  - Proof of principle: virtual satellites in RAM-SCB; virtual spectrograms
- Potential of virtual spacecraft in space weather models to prescribe the environment relevant to spacecraft charging

# Storm-time Inner Magnetosphere

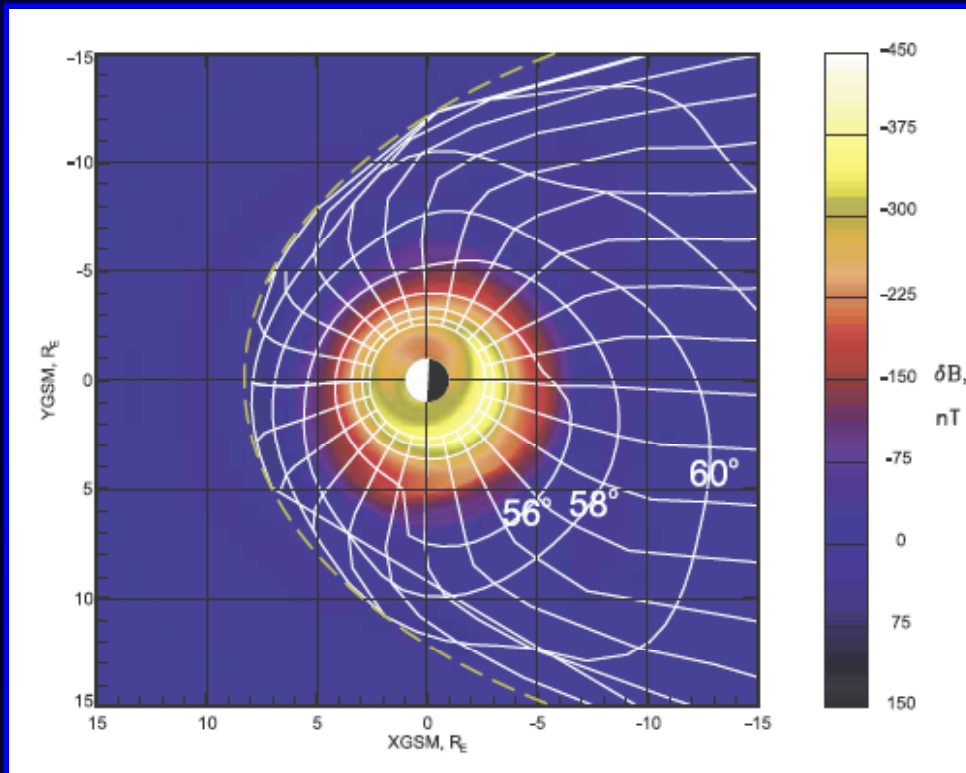


*From Daglis, [2006]*

- **Challenge:** to understand and model the space environment, specifically geomagnetic storm changes in the inner magnetosphere:
  1. Major changes in the geomagnetic field
  2. Ring current (keV to **10s of keV**) enhancement (→ **surface charging**)
  3. High-energy (MeV and **100s of keV**) electron flux enhancement (→ **internal charging**)
    - Affected by plasma-excited waves
    - **Dependent on the magnetic field**

# Dipole Approximation Breaks Down in the Storm-time Inner Magnetosphere

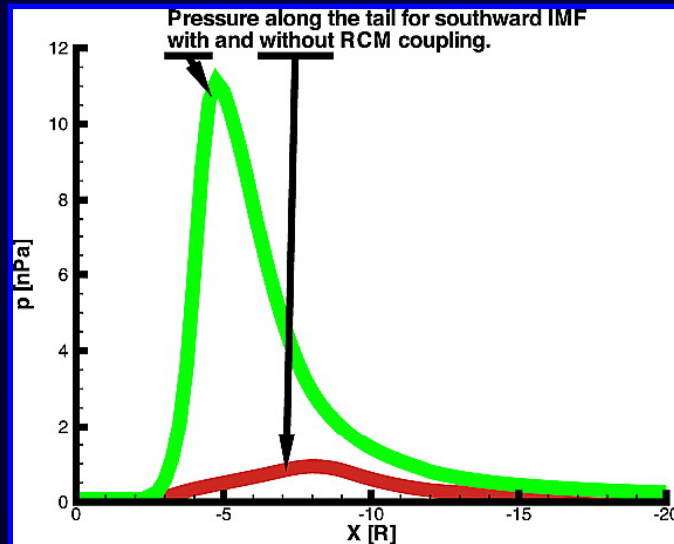
- Observations → strong magnetic field decrease during storms



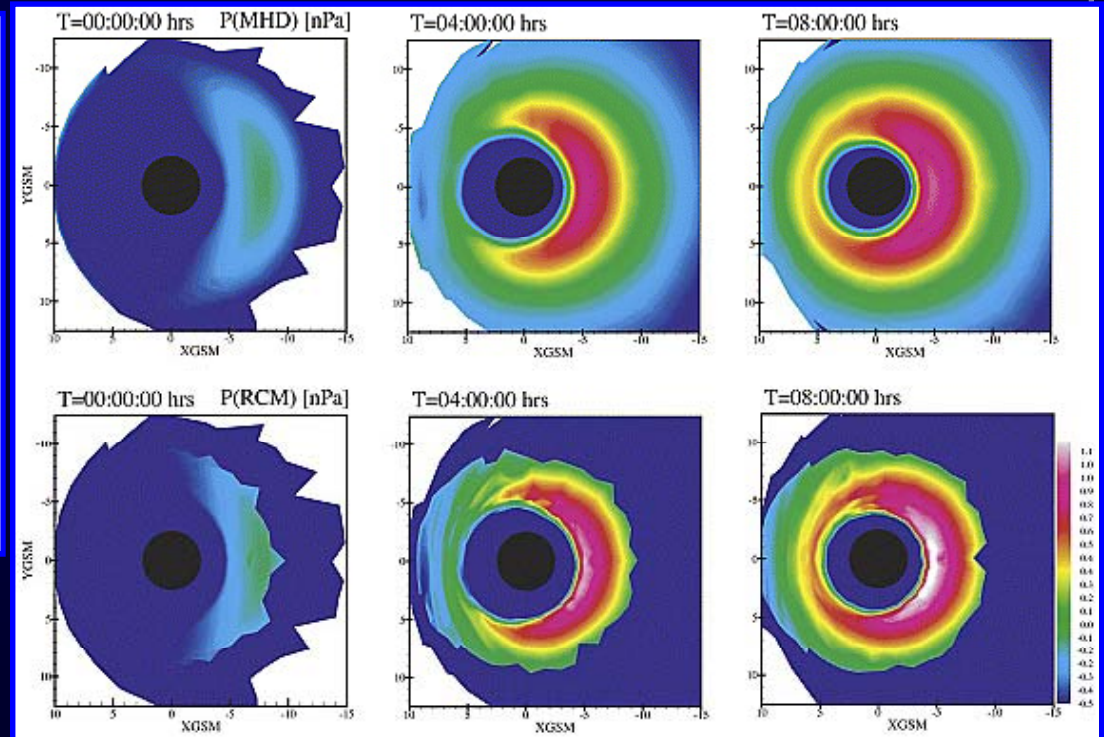
04/06/00 22:00 UT  $Dst = -250$  nT  
From *Tsyganenko et al., [2003]*

- Dipole approximation breaks down at  $3-4 R_E$
- The changed field significantly influences plasma/rad. belt particles

# Need for Physics-based Kinetic Models



*De Zeeuw et al., 2004*



- Plasma also changes the field
  - Global magnetohydrodynamics (MHD) models:
    - Fully self-consistent, but **unrealistic in inner magnetosphere**
    - Ring current energy density  $\sim 1/10^{\text{th}}$  of observed values
    - Causes: Coarse resolution; lack of gradient/curvature drifts and heat flux
- [Heinemann and Wolf, 2001]*

# RAM-SCB: Self-consistent Kinetic Inner Magnetosphere Model

## Ring current-atmosphere interactions model (RAM)

[Jordanova et al., 1994, 2006]

- Bounce-av. Boltzmann eq.
- Applied convective + corotation E-field
- Updated to general magnetic (B) field

Pressure



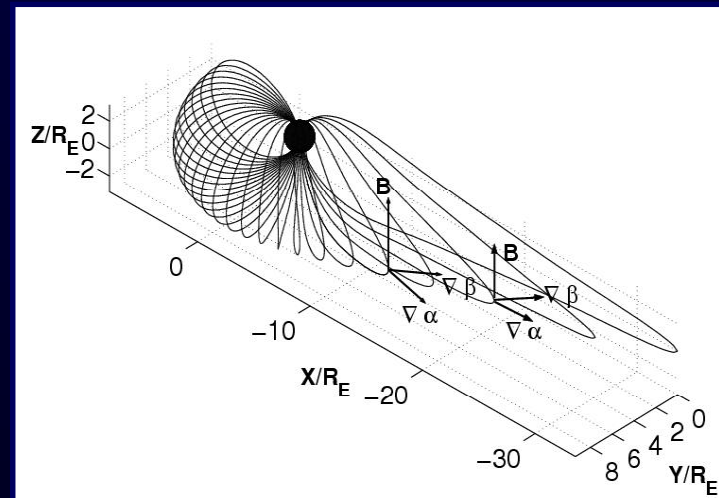
B-field



## 3D equilibrium code

[Cheng, 1995; Zaharia et al., 2004; Zaharia, 2008]

$$\mathbf{J} \times \mathbf{B} - \nabla \cdot \mathbf{P} = 0$$



- Euler potential formulation

# RAM-SCB Formalism: RAM

- RAM-SCB: particle/field dynamics on time scales  $>$  bounce/Alfven times
- Kinetic Ring Current Atmosphere Interactions Model (RAM):
  - Evolution of bounce-averaged distribution function [*Jordanova et al., 1994*]
  - Energy range: 100 eV to 500 keV
  - Generalized to arbitrary (closed-line) magnetic field geometry
  - 4 coordinates: 2 spatial (R,  $\varphi$ ) + energy E, pitch angle  $\alpha$  ( $\mu_0 = \cos \alpha$ )

$$\begin{aligned} \left\langle \frac{dF_t}{dt} \right\rangle &= \frac{\partial F_t}{\partial t} + \frac{1}{R_o^2} \frac{\partial}{\partial R_o} \left( R_o^2 \left\langle \frac{dR_o}{dt} \right\rangle F_t \right) + \frac{\partial}{\partial \varphi} \left( \left\langle \frac{d\varphi}{dt} \right\rangle F_t \right) + \\ &\frac{1}{\sqrt{E}} \frac{\partial}{\partial E} \left( \sqrt{E} \left\langle \frac{dE}{dt} \right\rangle F_t \right) + \frac{1}{h(\mu_o) \mu_o} \frac{\partial}{\partial \mu_o} \left( h(\mu_o) \mu_o \left\langle \frac{d\mu_o}{dt} \right\rangle F_t \right) = \\ &= \left\langle \frac{dF_t}{dt} \right\rangle_{losses} \end{aligned}$$

- Most physically complete model; different losses: charge exchange, Coulomb collisions, wave-particle interactions, losses to atmosphere

# RAM-SCB Formalism: SCB

- Single-fluid plasma equation of motion:
- Plasma and fields in the near-Earth magnetosphere ( $< 10 R_E$ ) in quasi-force balance (slow-flow approximation; *Wolf, [1983]*)
- B-field in Euler potential representation:
- Coupled quasi-2D elliptic PDEs, solved iteratively [*Zaharia et al., 2004;2008*]

$$\rho \cdot \left[ \frac{\partial \mathbf{v}}{\partial t} + (\mathbf{v} \cdot \nabla) \mathbf{v} \right] = \mathbf{J} \times \mathbf{B} - \nabla \cdot \mathbf{P}$$

mass density      acceleration      force density

$$\mathbf{J} \times \mathbf{B} = \nabla \cdot \mathbf{P}$$

With  $\nabla \cdot \mathbf{P} = \nabla P_{\perp} - \nabla \cdot [(P_{\perp} - P_{\parallel}) \mathbf{b}\mathbf{b}]$

$$\Downarrow$$

$$\sigma \mathbf{J} \times \mathbf{B} = \nabla P_{\perp} - (\mathbf{B} \cdot \nabla \sigma) \mathbf{B} + (1 - \sigma) \nabla \left( \frac{B^2}{2} \right) \quad \text{Force balance equation}$$


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$$\sigma = 1 + \frac{P_{\perp} - P_{\parallel}}{B^2}$$

$$\nabla \times \mathbf{B} = \mu_0 \mathbf{J} \quad \text{Ampere's law}$$

$$\nabla \cdot \mathbf{B} = 0 \quad \text{No magnetic monopoles}$$

$$\nabla \cdot \mathbf{B} = 0 \Rightarrow \mathbf{B} = \nabla \alpha \times \nabla \beta$$

$\alpha, \beta$  = Euler potentials  
(Clebsch coordinates or flux coordinates)  
 $\alpha$  = magnetic flux function  
 $\beta$  = angle - like variable

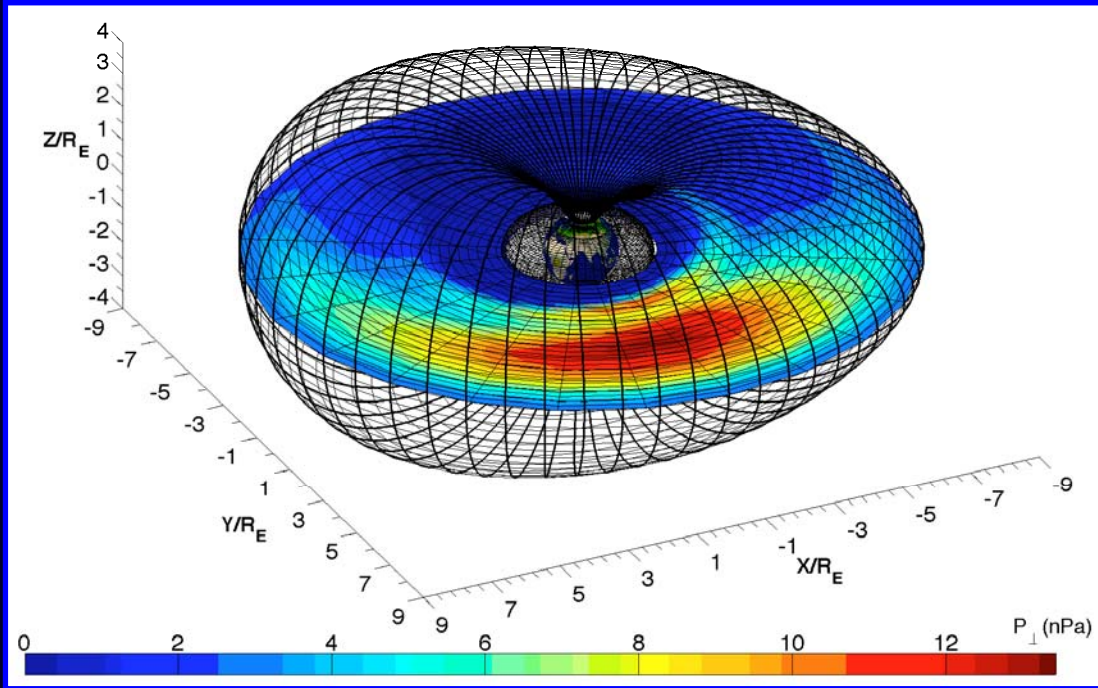
$$\sigma \nabla \cdot \left[ (\nabla \alpha)^2 \nabla \beta - (\nabla \alpha \cdot \nabla \beta) \nabla \alpha \right] = -\mu_0 \frac{\mathbf{B} \times \nabla \alpha}{B^2} \cdot \left[ \nabla P_{\perp} + (1 - \sigma) \nabla \left( \frac{B^2}{2} \right) \right]$$

$$\sigma \nabla \cdot \left[ (\nabla \alpha \cdot \nabla \beta) \nabla \beta - (\nabla \beta)^2 \nabla \alpha \right] = \mu_0 \frac{\mathbf{B} \times \nabla \beta}{B^2} \cdot \left[ \nabla P_{\perp} + (1 - \sigma) \nabla \left( \frac{B^2}{2} \right) \right]$$



# RAM-SCB Model Setup

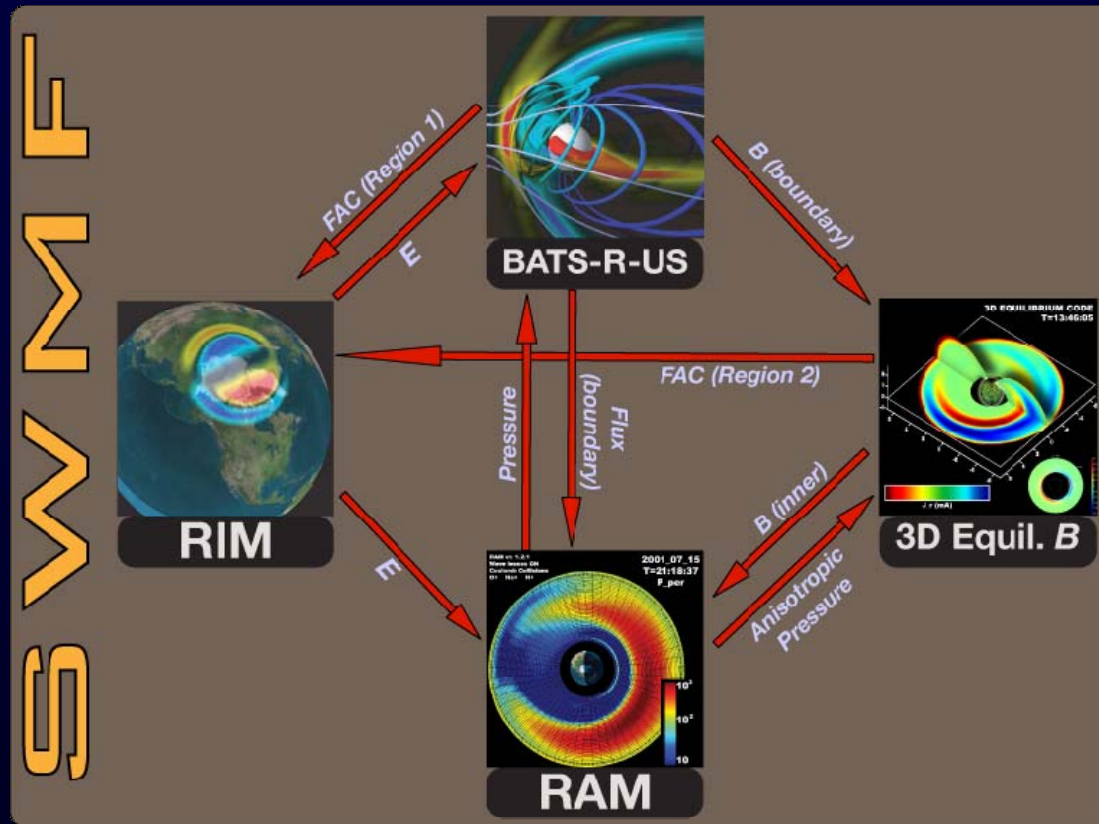
$$\mathbf{B} = \nabla \alpha \times \nabla \beta$$



RAM-SCB domain (T89 boundary)

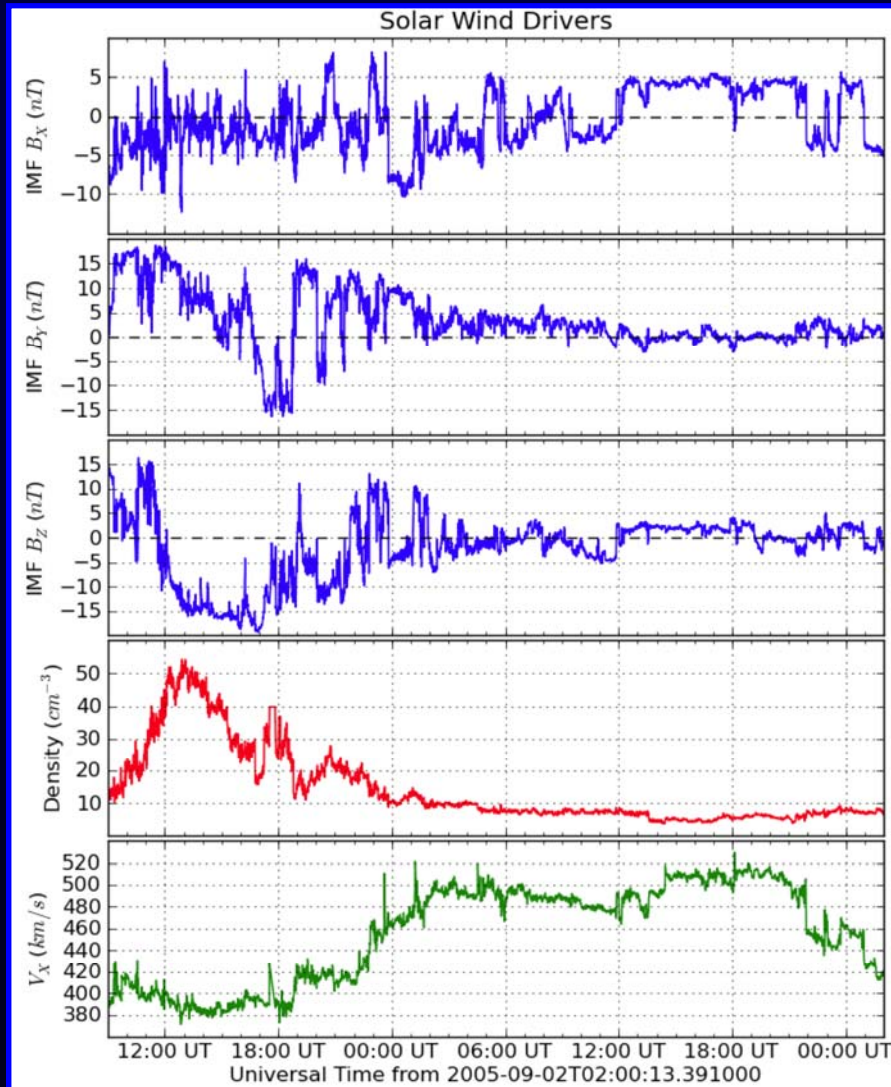
- Coupling freq.: 5 min.
- Plasma sheet boundary:
  - 6.6 R<sub>E</sub> – LANL obs. (MPA/SOPA)
  - Empirical plasma models/global codes (BATSRUS MHD)
- B-field boundary:
  - Empirical (T89, T04S)
  - BATSRUS MHD code
- E-field: empirical (Volland/Stern, Weimer) or from IE model
- Dipole tilt included (RAM in equatorial SM plane)

# RAM-SCB Inside Space Weather Modeling Framework (SWMF)



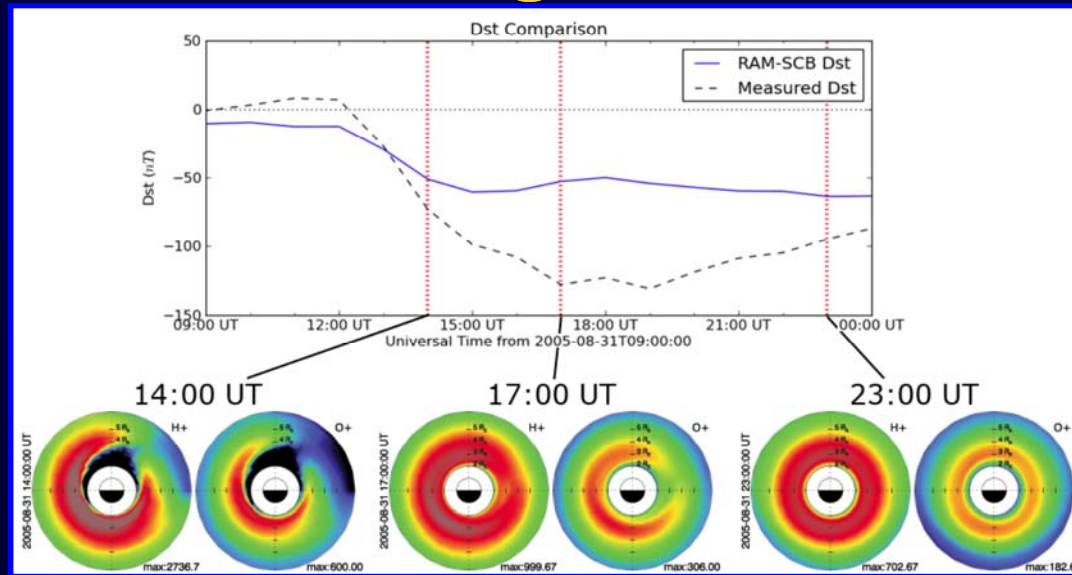
- Alternative RAM-SCB input: **plasma & magnetic boundaries** from BATS-R-US, **electric potentials** from ionospheric electrodynamics (IE) solver [Zaharia et al., submitted to *J. Geophys. Res.*, 2010]

# Simulated Event: Sep. 2005 Geomagnetic Storm



- Aug. 31, 2005 large CME-driven storm; min. SYM-H = -116 nT
- Main phase /early recovery (9:00 UT to 24:00 UT) simulated
- RAM-SCB inputs:
  - Plasma conditions at outer boundary by LANL geo. obs.
  - Ion composition by Young et al. [1982] empirical relationship:
$$n_{O^+}/n_{H^+} = 4.5 \times 10^{-2} \exp [0.17 Kp + 0.010 F_{10.7}]$$
- Convection electric field: Weimer 2001 empirical model
- B-field boundary by the T89 empirical model

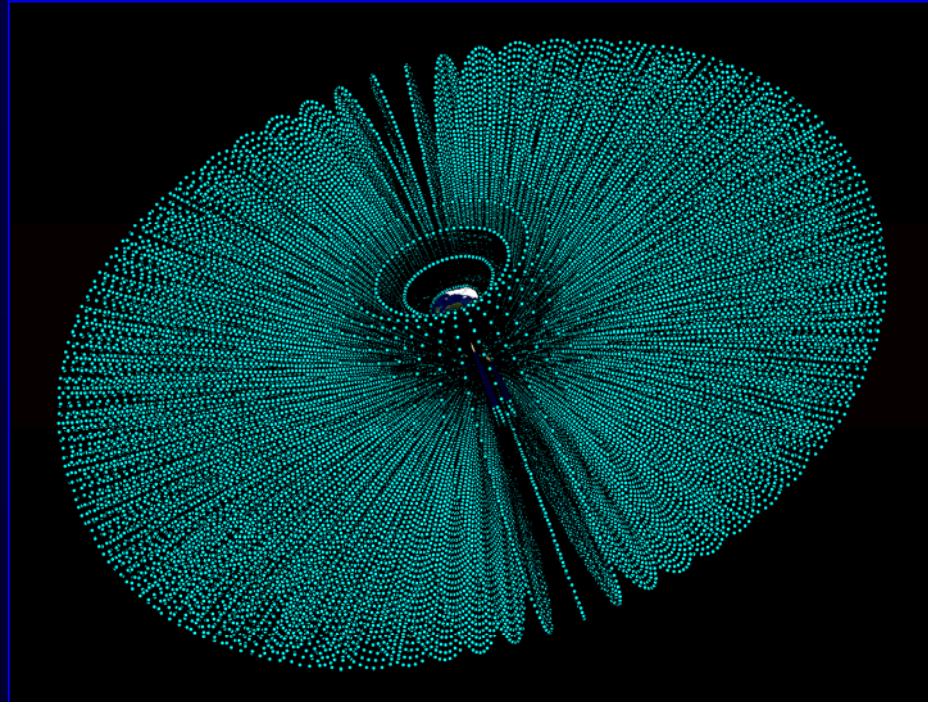
# Results – Ring Current and Dst



- Contribution to ring current by H+ and O+ for 3 times: early storm (14:00 UT), observed Dst peak (17:00 UT), early recovery (23:00 UT)
- RAM-SCB underpredicts the total ring current energy (and Dst)
  - Dst obtained with Dessler-Parker-Sckopke (DPS) formula from energy density inside geosynchronous orbit only
  - Magnetotail current contribution (up to 50% e.g. *Ganushkina et al., [2004]*) not included

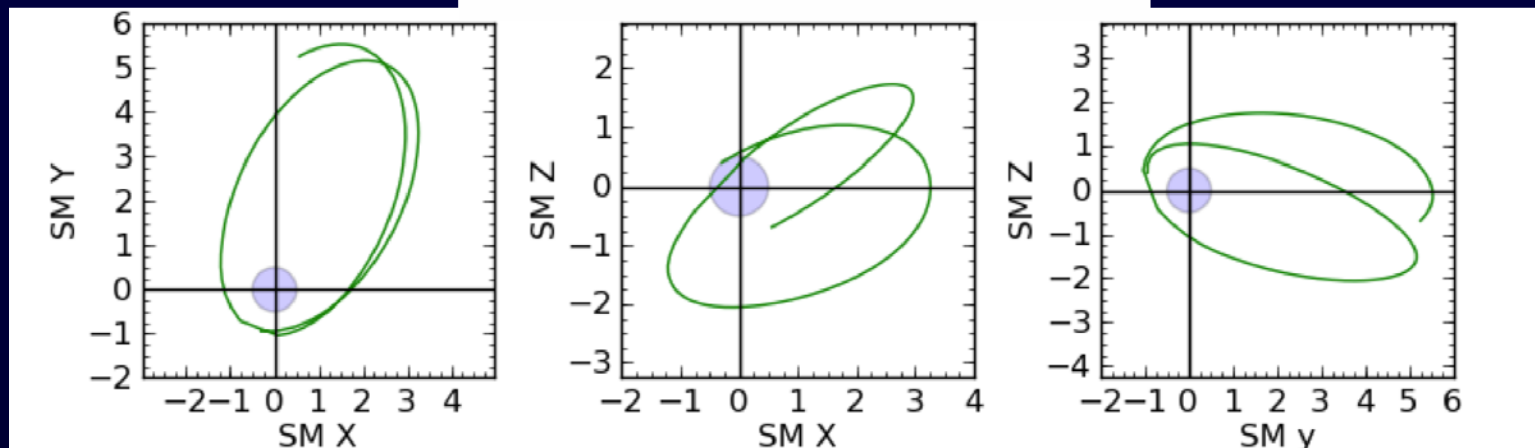
# Results at Virtual Spacecraft Locations

- Output from RAM-SCB – inside irregular 3-D cloud
  - Post-processing needed for output at each location of interest



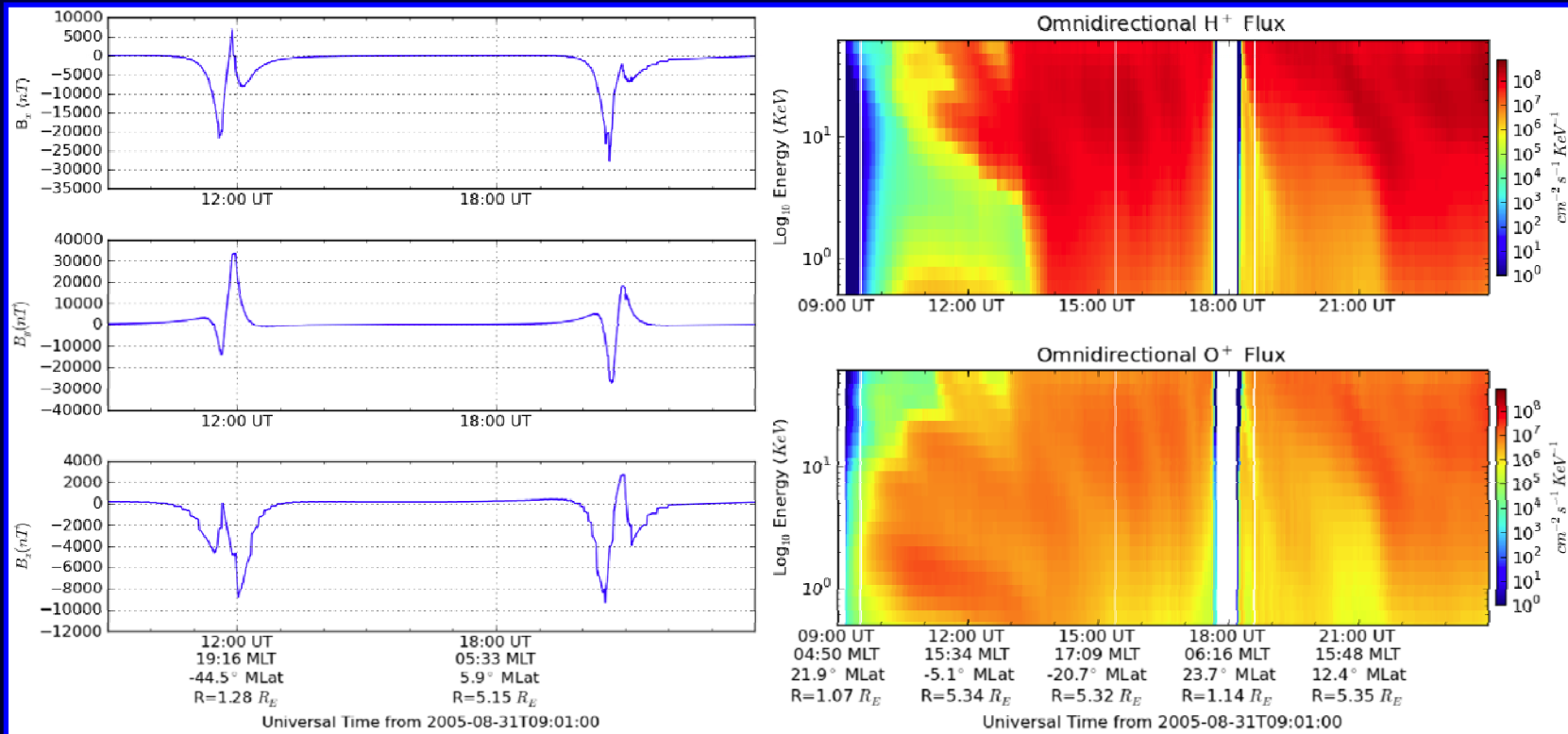
- Or: “fly” spacecraft in the simulation, obtain output at satellite location directly:
  1. For each point on satellite orbit, find grid nearest neighbors by k-d tree (octree) search method [Kennel, 2004]
  2. Interpolate (distance-weighted) among a set number of nearest neighbors
  3. For particle flux, use Liouville’s theorem to map distribution function from SM equatorial plane to all locations within 3-D domain

# Results: RBSP Virtual Spacecraft



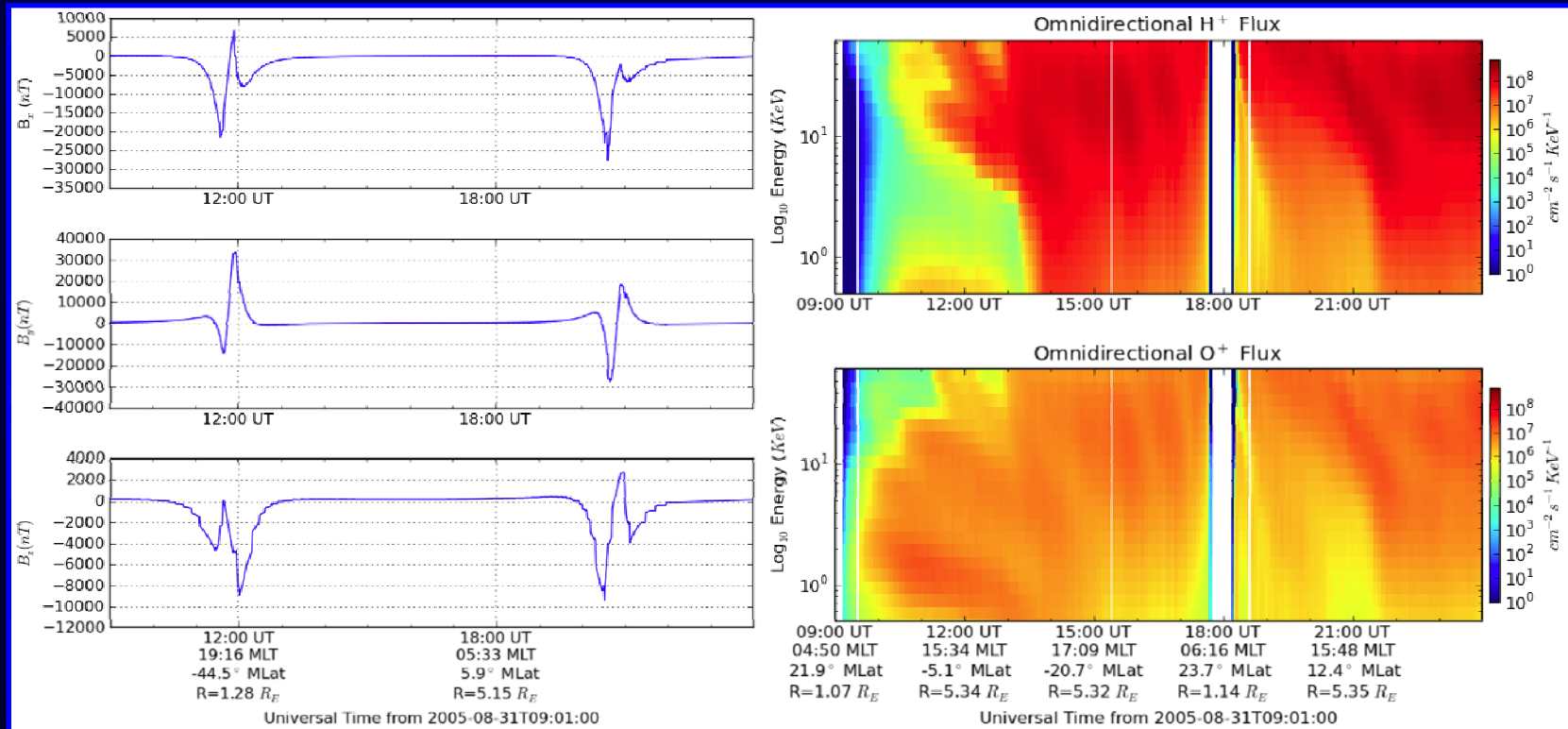
- Radiation Belt Storm Probes (RBSP)
  - slated to launch in 2012
  - 2-spacecraft mission will examine the radiation belts in-depth, including waves, magnetic and electric fields, and plasmas of ring current energies
- RBSP satellites included to **examine what they would observe had they been in orbit for this event**; using a portion of their early mission orbits
  - RBSP 1 spends most of the storm main phase in the noon/dusk quadrant; RBSP 2 lags behind slightly

# Results: Spacecraft-Specific (1)



- Magnetic field at RBSP 1 on left
- Fields are obtained at spacecraft location by interpolating from 8 nearest neighbor grid points to satellite location

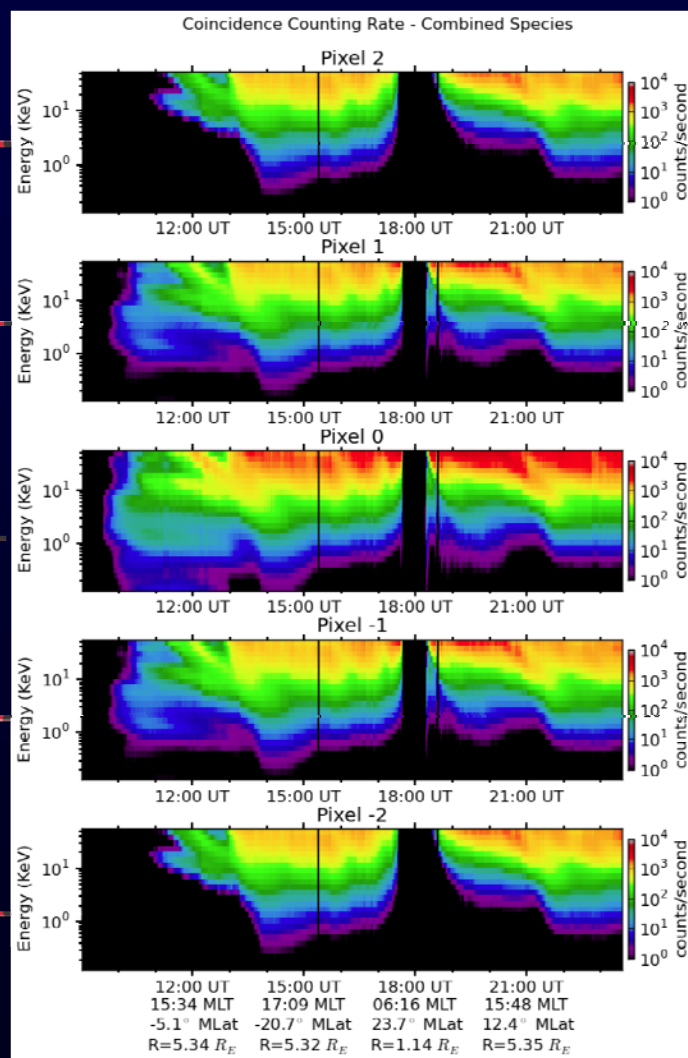
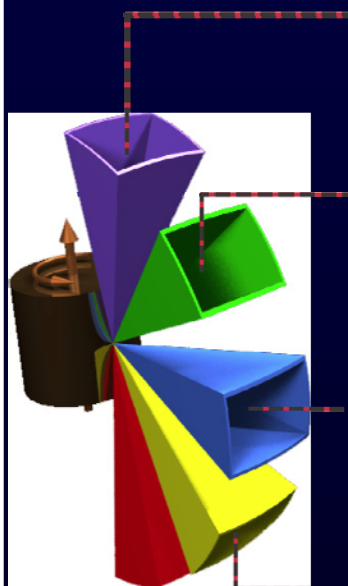
# Results: Spacecraft-Specific (2)



- Omnidirectional flux for  $H^+$  and  $O^+$  at RBSP 1 for RAM energies (100 eV to 500 KeV)
- Results “drop out” (e.g. 17:30 UT) when satellite leaves the simulation domain or when the grid nearest neighbors are beyond a set threshold

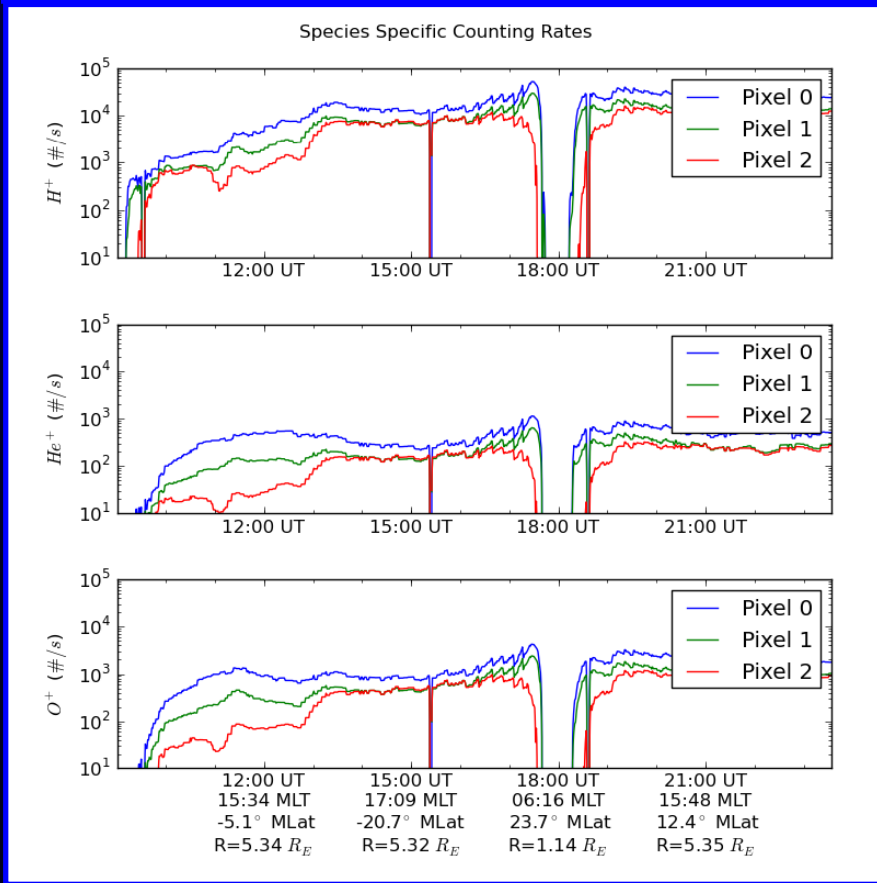
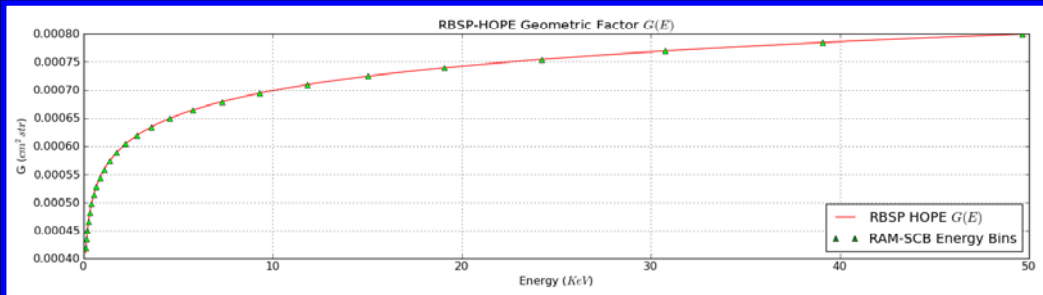


# Results: Instrument-Specific, Combined Species



- Helium, Oxygen, Proton, Electron (HOPE) instrument on RBSP:
  - ions/e- from 1 eV to 50 KeV
  - 5 separate polar pixels
- Coincidence counting rates from directional flux:
 
$$C = J * G * dE$$
  - J = directional flux
  - G = geometric factor
  - dE = width of energy bin
- RAM-SCB virtual satellite → count rates for each pixel

# Results: Instrument & Species-specific



- Spacecraft spin axis assumed parallel to local B
- RAM-SCB is gyrotropic  
→ results spin averaged
- RAM-SCB symmetric about 90° pitch angle  
→ pixels +/- 1 and 2 equivalent

# Summary

- Motivation: To quantify space environment output at specific spacecraft from numerical space weather model
- Tool: RAM-SCB physics-based self-consistent inner magnetosphere model: kinetic model + 3D force balance code
- Results:
  - Proof of principle: technique of “flying” virtual satellites in RAM-SCB successfully developed/used to generate high-res. results along spacecraft orbit (RBSP)
  - Satellite-specific simulation results used to create instrument-specific count rates/virtual spectrograms
  - Method applied to the RBSP HOPE instrument to create a mock-up of low-level data products

# Virtual Satellites in Numerical Models

- “Virtual” satellites – powerful method to tie observations and simulations together
- Use of virtual satellites - many research and applications possibilities:
  - Obtain ambient space environment for spacecraft charging models
  - Perform one-to-one model-observation comparisons
  - Complement existing observations with virtual set not bound by instrument restrictions
  - Plan for future missions with data product mock-ups/observation predictions
  - Monitor spacecraft-specific environmental conditions with real-time simulations

# Future Plans

- Model improvements:
  - Expand boundary to 9 or 10  $R_E$  (to obtain geosynchronous model output)
  - Include electrons to RAM-SCB simulation
  - Develop real-time version and validate/determine performance vs. input parameters
- Virtual satellite technique improvements:
  - Allow B-field and spacecraft spin axis to be non-parallel
  - Use geometric factors that vary in look angle and across the detector
  - Expand the number of instruments simulated
- Use model environment output in spacecraft charging code (e.g. NASCAP-2K)